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*The Cubic Character of the Tribonacci Roots,*  
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**Abstract**

If  $\tau$  is any root of the Tribonacci polynomial  $t(x) = x^3 - x^2 - x - 1$  in the Galois field  $\mathbb{F}_p$  where  $p$  is a prime,  $p \equiv 1 \pmod{3}$ , then

$$\tau^{\frac{p-1}{3}} \equiv 2^{\frac{2(p-1)}{3}} \pmod{p}.$$

More generally, if  $\chi$  is a root of  $t(x)$  in any field extension  $\mathbb{G}$  of  $\mathbb{F}_p$ , then  $2\chi$  is a cubic residue of the field  $\mathbb{G}$ .