Lawrence Somer and Michal Křížek
Iteration of Certain Arithmetical Functions of Particular Lucas Sequences,
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#### Abstract

Let $u(a, b)$ be a Lucas sequence satisfying the second-order recursion relation $u_{n+2}=a u_{n+1}+b u_{n}$, where $b= \pm 1, a$ is an integer, and $u_{0}=0$ and $u_{1}=1$. Let $m$ be a positive integer, and let $\pi(m)$ denote the period of $u(a, b)$ modulo $m$, and $\rho(m)$ denote the restricted period of $u(a, b)$ modulo $m$. It is shown that iterates of $\pi(m)$ and $\rho(m)$ end in either a fixed point or a cycle of length two, and all these possible fixed points and two-cycles are explicitly determined.


