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Iteration of Certain Arithmetical Functions of Particular Lucas Sequences,

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## Abstract

Let u(a, b) be a Lucas sequence satisfying the second-order recursion relation  $u_{n+2} = au_{n+1} + bu_n$ , where  $b = \pm 1$ , a is an integer, and  $u_0 = 0$ and  $u_1 = 1$ . Let m be a positive integer, and let  $\pi(m)$  denote the period of u(a, b) modulo m, and  $\rho(m)$  denote the restricted period of u(a, b) modulo m. It is shown that iterates of  $\pi(m)$  and  $\rho(m)$  end in either a fixed point or a cycle of length two, and all these possible fixed points and two-cycles are explicitly determined.