Salah Eddine Rihane, Bernadette Faye, Florian Luca, and Alain Togbé Powers of Two in Generalized Lucas Sequences,
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Abstract

For an integer $k \ge 2$, let $(L_n^{(k)})_n$ be the k-generalized Lucas sequence that starts with $0, \ldots, 0, 2, 1$ (k terms) and each term afterwards is the sum of the k preceding terms. In this paper, we find all powers of two that appear in k-generalized Lucas sequences; i.e., we study the Diophantine equation $L_n^{(k)} = 2^m$ in positive integers n, k, m with $k \ge 2$.