## Thomas Koshy

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## Abstract

We explore sums of gibonacci polynomial products of order 4 for  $g_{4n-1}, g_{4n}, g_{4n+1}, g_{4n+2}$ , and  $g_{4n+3}$  in terms of  $g_{n-2}^i, g_n^j$ , and  $g_{n+2}^k$ , where  $g_n$  denotes the *n*th gibonacci polynomial,  $0 \le i, j, k \le 4$ , and i+j+k = 4. Correspondingly, they yield formulas for  $G_{4n-1}, G_{4n}, G_{4n+1}, G_{4n+2}$ , and  $G_{4n+3}$ , where  $G_n$  denotes the *n*th gibonacci number. In addition, they have Pell implications.