John Greene, Junhyun Lim, Shaunak Mashalkar, and Edward F. Schaefer
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#### Abstract

Carmichael showed for sufficiently large $L, F_{L}$ has at least one prime divisor $p$ such that $p \equiv \pm 1(\bmod L)$. For a given $F_{L}$, we will show that a product of distinct odd prime divisors with this congruence condition is a Fibonacci pseudoprime. As a byproduct, this result leads to a proof of the presumably known result that if $L$ is prime and $F_{L}$ is composite, then $F_{L}$ is a Fibonacci pseudoprime. Such pseudoprimes can be used in an attempt, here unsuccessful, to find an example of a Baillie-PSW pseudoprime, i.e., an odd Fibonacci pseudoprime $n$ such that $n \equiv \pm 2(\bmod 5)$ and is also a base- 2 pseudoprime.


