John Greene, Junhyun Lim, Shaunak Mashalkar,
and Edward F. Schaefer
Using Fibonacci Factors to Create Fibonacci Pseudoprimes,
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Abstract

Carmichael showed for sufficiently large L, F_L has at least one prime divisor p such that $p \equiv \pm 1 \pmod{L}$. For a given F_L , we will show that a product of distinct odd prime divisors with this congruence condition is a Fibonacci pseudoprime. As a byproduct, this result leads to a proof of the presumably known result that if L is prime and F_L is composite, then F_L is a Fibonacci pseudoprime. Such pseudoprimes can be used in an attempt, here unsuccessful, to find an example of a Baillie-PSW pseudoprime, i.e., an odd Fibonacci pseudoprime n such that $n \equiv \pm 2 \pmod{5}$ and is also a base-2 pseudoprime.