

$$\begin{array}{r|l}
 3(n_{k-2} & n_{k-1} & 1 & n_1 & n_2 & \dots & 5 & 7 & 1 & 4 & 2 & 8) \\
 & & & & & & 7 & 1 & 4 & 2 & 8 & 4 \\
 & & & & & & 7 & 1 & 4 & 2 & 8 & 4 \\
 4(n_1 & n_2 & n_3 & n_4 & n_5 & \dots & 4 & 2 & 8 & 5 & 7 & 1)
 \end{array}$$

so that 428571 is a solution to our problem.

REFERENCES

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2. W. Page, "N-linked M-chains," *Mathematics Magazine*, Vol. 45 (March 1972), p. 101.
3. C.W. Trigg, "A Cryptarithm Problem," *Mathematics Magazine*, Vol. 45 (January 1972), p. 46.
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THE APOLLONIUS PROBLEM

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Problem 29 on page 216 of E.W. Hobson's *A Treatise on Plane Trigonometry*, Cambridge University Press (1918) reads: "Three circles, whose radii are a, b, c , touch each other externally; prove that the radii of the two circles which can be drawn to touch the three are

$$abc / [(bc + ca + ab) \pm 2\sqrt{abc(a + b + c)}]."$$

Horner [1] states "The formula...is due to Col. Beard" [2]. That the formula is incorrect is evident upon putting $a = b = c$, whereupon the radii become $a/(3 \pm 2\sqrt{3})$, so that one of them is negative. Horner recognized this when he stated, "The negative sign gives R (absolute value)...".

The correct formula has been shown [3] to be:

$$abc / [2\sqrt{abc(a + b + c)} \pm (ab + bc + ca)].$$

REFERENCES

1. Walter W. Horner, "Fibonacci and Apollonius," *The Fibonacci Quarterly*, Vol. 11, No. 5 (Dec. 1973), pp. 541-542.
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3. C.W. Trigg, "Corrected Solution to Problem 2293," *School Science and Math.*, 53 (Jan. 1953), p. 75.
