



The Fibonacci Quarterly

THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION

TABLE OF CONTENTS

On a New Kind of Numbers	<i>A.K. Agarwal</i>	194
Some Sequences of Large Integers	<i>Henry Ibstedt</i>	200
Characteristics and the Three Gap Theorem	<i>Tony van Ravenstein, Graham Winley and Keith Tognetti</i>	204
Announcement on Fourth International Conference on Fibonacci Numbers and Their Applications		214
A Two-Variable Lagrange-Type Inversion Formula with Applications to Expansion and Convolution Identities	<i>Christian Krattenthaler</i>	215
Lambert Series and the Summation of Reciprocals in Certain Fibonacci-Lucas-Type Sequences	<i>R. André-Jeannin</i>	223
Third International Conference Proceedings		226
The Distribution of Residues of Two-Term Recurrence Sequences	<i>Eliot Jacobson</i>	227
Generalizations of the Dual Zeckendorf Integer Representation Theorems—Discovery by Fibonacci Trees and Word Patterns	<i>J.C. Turner and T.D. Robb</i>	230
The Fibonacci Sequence and the Time Complexity of Generating the Conway Polynomial and Related Topological Invariants	<i>Phillip G. Bradford</i>	240
An Algebraic Identity and Some Partial Convolutions	<i>W.C. Chu</i>	252
On Certain Number-Theoretic Inequalities	<i>J. Sándor and L. Tóth</i>	255
Length of the n -Number Game	<i>Anne Ludington-Young</i>	259
Tiling the k^{th} Power of a Power Series	<i>J. Arkin, D.C. Arney, G.E. Bergum, S.A. Burr and B.J. Porter</i>	266
On a Hoggatt-Bergum Paper with Totient Function Approach for Divisibility and Congruence Relations	<i>Sahib Singh</i>	273
Elementary Problems and Solutions	<i>Edited by A.P. Hillman</i>	277
Advanced Problems and Solutions	<i>Edited by Raymond E. Whitney</i>	283

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PURPOSE

The primary function of **THE FIBONACCI QUARTERLY** is to serve as a focal point for widespread interest in the Fibonacci and related numbers, especially with respect to new results, research proposals, challenging problems, and innovative proofs of old ideas.

EDITORIAL POLICY

THE FIBONACCI QUARTERLY seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with new ideas that develop enthusiasm for number sequences or the exploration of number facts. Illustrations and tables should be wisely used to clarify the ideas of the manuscript. Unanswered questions are encouraged, and a complete list of references is absolutely necessary.

SUBMITTING AN ARTICLE

Articles should be submitted in the format of the current issues of **THE FIBONACCI QUARTERLY**. They should be typewritten or reproduced typewritten copies, that are clearly readable, double spaced with wide margins and on only one side of the paper. The full name and address of the author must appear at the beginning of the paper directly under the title. Illustrations should be carefully drawn in India ink on separate sheets of bond paper or vellum, approximately twice the size they are to appear in print. Since the Fibonacci Association has adopted $F_1 = F_2 = 1$, $F_{n+1} = F_n + F_{n-1}$, $n \geq 2$ and $L_1 = 1$, $L_2 = 3$, $L_{n+1} = L_n + L_{n-1}$, $n \geq 2$ as the standard definitions for The Fibonacci and Lucas sequences, these definitions *should not* be a part of future papers. However, the notations *must* be used.

Two copies of the manuscript should be submitted to: **GERALD E. BERGUM, EDITOR, THE FIBONACCI QUARTERLY, DEPARTMENT OF COMPUTER SCIENCE, SOUTH DAKOTA STATE UNIVERSITY, BOX 2201, BROOKINGS, SD 57007-0194.**

Authors are encouraged to keep a copy of their manuscripts for their own files as protection against loss. The editor will give immediate acknowledgment of all manuscripts received.

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DEVOTED TO THE STUDY
OF INTEGERS WITH SPECIAL PROPERTIES*

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