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Inverting A Finite Series with Constant Coefficients,
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Abstract

The purpose of this paper is to solve for $f(n)$ where

$$g_r(n) = \sum_{k=0}^{r} a_k f(n-k), \qquad (*)$$

where $f(n) = 0$ if $n < 0$, and $\{a_0, a_1, \ldots\}$ are constants. The main results are a recursive formula and an explicit formula for the inversion of the series defined by (*).