The number of permutations of order $n$ with no fixed points is called the $n$th derangement number, and is denoted by $D_n$. It is well-known that for $n > 1$, the derangement numbers satisfy the recurrence $D_n = nD_{n-1} + (-1)^n$. We present a simple combinatorial proof of this recurrence.