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*The Sums of the Consecutive Fibonacci Numbers*,
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**Abstract**

In this paper, we study integer numbers $d$ with the following property: the sum of any $d$ consecutive Fibonacci numbers is divisible by $d$. We call these $d$-numbers. We demonstrate a relation between $d$-numbers and the Pisano period, specifically, we prove that the original problem is equivalent to finding all integer numbers $d > 1$ that are divisible by their own Pisano period. We derive a general expression for all $d$-numbers and obtain convenient recurrent relations that significantly simplify practical calculation. Finally, we establish an equivalence between $d$-numbers and the OEIS sequence A072378.