

Hsin-Yun Ching, Rigoberto Flórez, F. Luca, Antara Mukherjee, and J. C. Saunders

Primes and Composites in the Determinant Hosoya Triangle,
Fibonacci Quart. **60** (2022), no. 5, 56–110.

Abstract In this paper, we look at numbers of the form $H_{r,k} := F_{k-1}F_{r-k+2} + F_kF_{r-k}$. These numbers are the entries of a triangular array called the *determinant Hosoya triangle* which we denote by \mathcal{H} . We discuss the divisibility properties of the above numbers and their primality. We give a small sieve of primes to illustrate the density of prime numbers in \mathcal{H} . Since the Fibonacci and Lucas numbers appear as entries in \mathcal{H} , our research is an extension of the classical questions concerning whether there are infinitely many Fibonacci or Lucas primes. We prove that \mathcal{H} has arbitrarily large neighbourhoods of composite entries. Finally we present an abundance of data indicating a very high density of primes in \mathcal{H} .