

## SUBJECT INDEX

This Index replaces the former Quick Reference Key Word Index. This Index provides sub topic listings for the larger categories . For example, generating functions has about 100 sub-listings.

Entries are listed by volume and issue number (page number) using the format **vol #.issue #(page #)** and the page reference is indicated by the **beginning** of the article in which the topic appears. Some topics have several sub categories and can be found under the specific heading. For example, most things relating to Pell such as equations, identities or polynomials are listed under Pell, not under equations, identities or polynomials, respectively. But in some cases appear under other specific headings.

Since the topic “Fibonacci” has an immense number of entries, it seemed prudent to segregate Fibonacci topics. Similarly for Lucas topics. So for the letter “F” all non-Fibonacci topic listings appear first, followed by listings “Fibonacci-A”, etc. Similarly for the letter “L” and “Lucas-A”, etc. Other topics are listed in a natural way.

Note that this Index is intended to be as complete as possible. However there are bound to be sins of omission, some intentional, some not. If you use this Index and are unable to find something, please inform the indexer at <[charliecook29150@aim.com](mailto:charliecook29150@aim.com)> so that any missing topic will be available in the next version submitted to the Fibonacci Home Page. Note that some duplication of entries exists.

Year references for each volume are as follows with the number of issues in parentheses.

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MRFS: 18th Anniversary Collection of Manuscripts Related to the Fibonacci Sequence (1980)

PI	1984 International Conference Proceedings (1986)
PII	1986 International Conference Proceedings (1988)
PIII	1988 International Conference Proceedings (1990)
PIV	1990 International Conference Proceedings (1991)
PV	1992 International Conference Proceedings (1993)
PVI	1994 International Conference Proceedings (1996)
PVII	1996 International Conference Proceedings (1998)

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PVIII	1998 International Conference Proceedings (1999)
PIX	2002 International Conference Proceedings (2004)*
PXI	2004 International Conference Proceedings (2009)
PXII	2006 International Conference Proceedings (2010)
PXIII	2008 International Conference Proceedings (2010)
PXIV	2010 International Conference Proceedings (2011)
PXV	2012 International Conference Proceedings (2013)
PXVI	2014 International Conference Proceedings (2014)
PXVII	2016 International Conference Proceedings (2017)
PXVIII	2018 International Conference Proceedings (2019)
PXIX:	2020 University of Sarajevo, Bosnia and Herzegovina 7/20-25/2020 (On Line: <i>TFQ</i> Issues on The Fibonacci Association Home Page)

\* No Proceedings were printed for the 2000 International Conference. So PIX refers to the 10th International Conference, etc.

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