

Then in terms of the Riemann Zeta function,

$$-C_n = \frac{1}{n^s} + \frac{1}{n^{s+1}} + \frac{1}{n^{s+2}} + \dots$$

or

$$C_n = \left\{ \frac{1}{1^s} + \frac{1}{2^s} + \frac{1}{3^s} + \frac{1}{(n-1)^s} \right\} - \zeta(s).$$

However, the zeta function can be analytically continued for  $\operatorname{Re}(s) < 1$  and for negative integers it is given by [2]

$$\zeta(-2m) = 0, \quad \zeta(1-2m) = (-1)^m B_m / (2m), \quad m = 1, 2, 3, \dots,$$

$$\zeta(0) = -1/2 \quad (B_m \text{ are the Bernoulli numbers}).$$

Now letting  $s = -1$  above, gives the valid particular solution

$$C_n = (1 + 2 + 3 + \dots + n - 1) - \zeta(-1).$$

Since the constant  $\zeta(-1)$  satisfies the homogeneous equation, it can be deleted.

#### REFERENCES

1. R. J. Weinschenk and V. E. Hoggatt, Jr., "On Solving  $C_{n+2} = C_{n+1} + C_n + n^m$  by Expansions and Operators," *Fibonacci Quarterly*, Vol. 8, No. 1, 1970, pp. 39-48.
2. C. N. Watson, *A Course in Modern Analysis*, Cambridge University Press, Cambridge, 1946, pp. 267-268.



[Continued from page 162.]

#### ERRATA

Please make the following correction to "A New Greatest Common Divisor Property of the Binomial Coefficients," appearing on p. 579, Vol. 10, No. 6, Dec. 1972:

On page 584, last equation, for

$$\binom{n+n}{k+a} \quad \text{read} \quad \binom{n+a}{k+a}.$$

In "Some Combinatorial Identities of Bruckman," appearing on page 613 of the same issue, please make the following correction.

On the right-hand side of Eq. (12), p. 615, for

$$\frac{2k}{2k+1} \quad \text{read} \quad \frac{2^k}{2k+1}.$$

