

REFERENCES

1. A. H. Beiler, "Consecutive Hypotenuses of Pythagorean Triangles," UMT 74, *Math. Comp.*, Vol. 22, 1968, pp. 690-692.
2. Thomas H. Southard, *Addition Chains for the First n Squares*, Center Numerical Analysis, CNA-84, Austin, Texas, 1974.
3. Daniel Shanks, "The Second-Order Term in the Asymptotic Expansion of $B(x)$," *Math. Comp.*, Vol. 18, 1964, pp. 75-86.
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[Continued from P. 318.]

$$(1/-1) = 1,$$

$$(-1/1) = 1,$$

$$(1/1) = 1.$$

The second entry of the Extended Jacobi Symbol is multiplicative by definition; it will be proved in the corollaries that both entries are also periodic.

The following results are easily derived:

Explicitly,

$$(0/1) = 1,$$

$$(0/b) = 0 \text{ if } b \neq 1,$$

$$(0/-b) = 0 \text{ if } -b \neq 1,$$

$$(2/\pm b) = (-1)^{(b^2-1)/8},$$

$$(-2/b) = (-1)^{(b^2+4b-5)/8},$$

$$(-2/-b) = (-1)^{(b^2-4b-5)/8}.$$

If $a \neq 0$, then

$$(-a^2/-1) = -1,$$

$$(-1/-b^2) = -1;$$

$$(-a/1) = 1,$$

$$(a/-1) = (a/-1) \text{ (see below),}$$

$$(-a/-1) = -(a/-1);$$

$$(1/b) = 1,$$

$$(-1/b) = (-1)^{(b-1)/2},$$

$$(1/-b) = 1,$$

$$(-1/-b) = (-1)^{(b+1)/2}.$$

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