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### ON THE FORMULA $\pi = 2\sum \text{arccot } f_{2k+1}$

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While questing the  $n + 1^{\text{st}}$  digit of  $\pi$ ,  
With series by Taylor, MacLauren, et al;  
I tried the arccotan of integers high,  
While old Leonardo de Pisa did call.

Old friends are a joy and, at times, a surprise  
When they serendipitously drop by to chat.  
They lighten our labors and open our eyes.  
"Eureka!" quoth I. "Now, how about that!"

For what to my wondering eyes should appear,  
Intermix't with the spurious inverse cotans,  
Were eight Fibonacci terms standing right here,  
Waiting and patiently holding their hands.

The even term's arccotangent's easily seen  
to equal the sum of the next pair in line.  
Now start back with  $\pi$ , and keep your eyes keen  
It makes 4 arccotan the unit sublime.

Note: 1 is the first and the second old friend.  
So rewrite:  $\pi$  equals twice this plus twice that.  
"This" is the arccot of the first term of Len.  
"That," which we'll split, is from the second old hat.

From 2 we get 3, 4; from 4, 5 and 6.  
The evens keep splitting; the odds hang behind.  
Forming convergent series: sum twice arccot  $f$   
Sub  $2k + 1$  which is  $\pi$ , I remind.

We don't know the digit half-million and one.  
Guinness, keep stout! There'll be other tries.  
I've got half my friends in a pretty new sum.  
Well worth the labor to open my eyes.