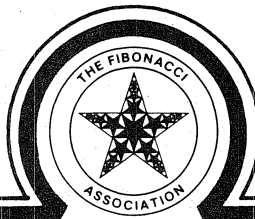


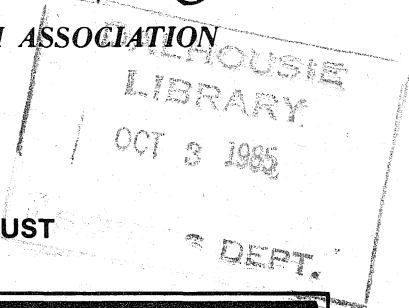
# The Fibonacci Quarterly

THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION

VOLUME 23  
NUMBER 3



AUGUST  
1985



## CONTENTS

|   |   |     |
|---|---|-----|
| A Third-Order Analog of a Result<br>of L. Carlitz .....                             | <i>Vichian Laohakosol &amp; Nit Roenrom</i>                             | 194 |
| Generalized Fibonacci Numbers and Some<br>Diophantine Equations .....               | <i>Jannis A. Antoniadis</i>   | 199 |
| Zigzag Polynomials .....  | <i>A.F. Horadam</i>   | 214 |
| On a Fibonacci Arithmetical Trick .....   | <i>Calvin T. Long</i>   | 221 |
| A Fibonacci Sequence of<br>Distributive Lattices .....                              | <i>Hartmut Höft &amp; Margret Höft</i>                                  | 232 |
| A Note on the Sums of Fibonacci and<br>Lucas Polynomials .....                      | <i>Blagoj S. Popov</i>  | 238 |
| Jacobsthal Polynomials and a Conjecture Concerning Fibonacci-Like<br>Matrices ..... | <i>C.E. Bergum, Larry Bennett, A.F. Horadam, &amp; S.D. Moore</i>       | 240 |
| Integers Related to the Bessel Function $J_1(z)$ .....                              | <i>F.T. Howard</i>  | 249 |
| The Number of Spanning Trees in the Square of a Cycle<br>.....                      | <i>G. Baron, F.T. Boesch, H. Prodinger, R.F. Tichy, &amp; J.F. Wang</i> | 258 |
| A Ratio Associated<br>with $\phi(x) = n$ .....                                      | <i>Kenneth B. Stolarsky &amp; Steven Greenbaum</i>                      | 265 |
| Hyperperfect and Unitary Hyperperfect<br>Numbers .....                              | <i>Walter E. Beck &amp; Rudolph M. Najar</i>                            | 270 |
| Announcement .....  |   | 276 |
| Elementary Problems and Solutions<br>.....  | <i>Edited by A.P. Hillman, Gloria C. Padilla, &amp; Charles R. Wall</i> | 277 |
| Advanced Problems and Solutions .....   | <i>Edited by Raymond E. Whitney</i>                                     | 282 |

## PURPOSE

The primary function of **THE FIBONACCI QUARTERLY** is to serve as a focal point for widespread interest in the Fibonacci and related numbers, especially with respect to new results, research proposals, challenging problems, and innovative proofs of old ideas.

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**THE FIBONACCI QUARTERLY** seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with new ideas that develop enthusiasm for number sequences or the exploration of number facts. Illustrations and tables should be wisely used to clarify the ideas of the manuscript. Unanswered questions are encouraged, and a complete list of references is absolutely necessary.

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All back issues of **THE FIBONACCI QUARTERLY** are available in microfilm or hard copy format from **UNIVERSITY MICROFILMS INTERNATIONAL, 300 NORTH ZEEB ROAD, DEPT. P.R., ANN ARBOR, MI 48106.** Reprints can also be purchased from **UMI CLEARING HOUSE** at the same address.

1984 by

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# *The Fibonacci Quarterly*

Founded in 1963 by Verner E. Hoggatt, Jr. (1921-1980)  
Br. Alfred Brousseau, and I.D. Ruggles

*THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION  
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