



# The Fibonacci Quarterly

THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION

## TABLE OF CONTENTS

A Congruence for Fibonomial Coefficients Modulo $p^3$ .....	<i>William A. Kimball and William A. Webb</i>	290
Visualizing Golden Ratio Sums with Tiling Patterns .....	<i>Marjorie Bicknell-Johnson and Duane DeTemple</i>	298
Seventh International Research Conference .....		303
Proof of a Result by Jarden by Generalizing a Proof by Carlitz .....	<i>Curtis Cooper and Robert E. Kennedy</i>	304
A Note Regarding Continued Fractions .....	<i>Neville Robbins</i>	311
Book Announcement: Generalized Pascal Triangles and Pyramids: Their Fractals, Graphs and Applications.....	<i>by Dr. Boris Bondarenko</i>	312
Ducci-Sequences and Pascal's Triangle.....	<i>Herbert Glaser and Gerd Schöffl</i>	313
Author and Title Index for Sale.....		324
Some Probabilistic Aspects of the Terminal Digits of Fibonacci Numbers .....	<i>Piero Filippini and Renato Menicocci</i>	325
On an Arithmetical Function Related to Euler's Totient and the Discriminator .....	<i>Pieter Moree and Hans Roskam</i>	332
A Note on a General Class of Polynomials, Part II .....	<i>Richard André-Jeannin</i>	341
Squares of Second-Order Linear Recurrence Sequences .....	<i>Tom C. Brown and Peter Jau-shyong Shiue</i>	352
Dynamics of the Mapping $f(x) = (x + 1)^{-1}$ .....	<i>Paul Bracken</i>	357
Fifth International Conference Proceedings .....		358
Recurrence Sequences and Bernoulli Polynomials of Higher Order .....	<i>Zhang Zhizheng and Guo Lizhou</i>	359
A Disjoint Covering of the Set of Natural Numbers Consisting of Sequences Defined by a Recurrence Whose Characteristic Equation Has a Pisot Number Root.....	<i>Shiro Ando and Teluhiko Hilano</i>	363
Antisocial Dinner Parties.....	<i>Richard Lewis</i>	368
Elementary Problems and Solutions .....	<i>Edited by Stanley Rabinowitz</i>	371
Advanced Problems and Solutions.....	<i>Edited by Raymond E. Whitney</i>	378

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## PURPOSE

The primary function of **THE FIBONACCI QUARTERLY** is to serve as a focal point for widespread interest in the Fibonacci and related numbers, especially with respect to new results, research proposals, challenging problems, and innovative proofs of old ideas.

## EDITORIAL POLICY

**THE FIBONACCI QUARTERLY** seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with new ideas that develop enthusiasm for number sequences or the exploration of number facts. Illustrations and tables should be wisely used to clarify the ideas of the manuscript. Unanswered questions are encouraged, and a complete list of references is absolutely necessary.

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DEVOTED TO THE STUDY  
OF INTEGERS WITH SPECIAL PROPERTIES*

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