

THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION

# **TABLE OF CONTENTS**

Almost Square Triangular Numbers K. B. Subramaniam	194
Note on the Pierce Expansion of	
a Logarithm P. Viader, J. Paradis and L. Bibiloni	198
Author and Title Index	202
Generalized Fibonacci Sequences and A Generalization of the O-Matrix Thizheng Thang	203
Naw Droklam Wak Site	203
New Problem web She	207
Lambert Series and Elliptic Functions and Certain Reciprocal Sums	208
Generalized Fibonacci and Lucas Polynomials, and Their Associated	
Diagonal Polynomials	213
On ∞-Generalized Fibonacci Sequences W. Motta, M. Rachidi and O. Saeki	223
Generalized Bracket Function Inverse Pairs	233
Partial Fibonacci and Lucas Numbers Indulis Strazdins	240
Sums of Certain Products of Fibonacci and Lucas Numbers R. S. Melham	248
Fibonacci Numbers and Harmonic Quadruples Georg J. Rieger	252
Notes on Reciprocal Series Related to Fibonacci	
and Lucas Numbers Feng-Zhen Zhao	254
On the Form of Solutions of Martin Davis'	
Diophantine Equation Anatoly S. Izotov	258
On the Integers of the Form $n(n-1)-1$ P. Filipponi and O. Brugia	262
Announcement of the Ninth International Conference	
on Fibonacci Numbers and Their Applications	264
Arithmetic Functions of Fibonacci Numbers	265
Lucas Sequences and Functions of a 4-by-4 Matrix R. S. Melham	269
Elementary Problems and Solutions Edited by Stanley Robinowitz	277
Advanced Problems and Solutions Edited by Raymond E. Whitney	282

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# PURPOSE

The primary function of **THE FIBONACCI QUARTERLY** is to serve as a focal point for widespread interest in the Fibonacci and related numbers, especially with respect to new results, research proposals, challenging problems, and innovative proofs of old ideas.

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**THE FIBONACCI QUARTERLY** seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with new ideas that develop enthusiasm for number sequences or the exploration of number facts. Illustrations and tables should be wisely used to clarify the ideas of the manuscript. Unanswered questions are encouraged, and a complete list of references is absolutely necessary.

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