## LINEAR RECURSION RELATIONS

## PROBLEMS

1. Prove that

$$L_{2n} = L_n^2 + 2(-1)^{n+1}$$

2. Using the Binet formulas, find the value of:

$$L_n F_{n-1} - F_n L_{n-1}$$
.

3.	$F_{3n} = F_n($	).	Determine the expression for the cofactor of $F_{n^{\circ}}$
4.	$F_{5n} = F_n($	).	Determine the expression for the cofactor of $F_n$ .
5.	$L_{3n} = L_n($	).	Find the expression for the cofactor of $L_n$ .
6.	$L_{5n} = L_{n}$ (	).	Find the expression for the cofactor of $L_n$ .
7.	For the Fibona	acci relat	tion with $T_1 = 3$ , $T_2 = 7$ , find the expression for

 $\boldsymbol{T}_n$  in terms of powers of  $\boldsymbol{r}$  and  $\boldsymbol{s}.$ 

- 8. Using the binomial expansion, find an expression for  $F_n$  in terms of powers of 5 and binomial coefficients.
- 9. Do likewise for L<sub>n</sub>.
- 10. Assuming the relation

$$L_{n} + L_{n+2} = 5F_{n+1}$$
,

determine an equivalent single Fibonacci number for  $F_n^2 + F_{n+1}^2$  using the Binet formula.

[Continued on p. 106.]

## ERRATA FOR

## A LINEAR ALGEBRA CONSTRUCTED FROM FIBONACCI SEQUENCES

J. W. GOOTHERTS

Lockheed Missiles & Space Company, Sunnyvale, Calif.

Please make the following changes in the above-entitled article, appearing in Vol. 6, No. 5, November 1968:

On page 36, change the eighth line from the end to read: <u>Definition 1.5</u>. For  $U, V \in \mathcal{F}$ ,  $UV = (u_0v_0 + u_1v_1, u_0v_1 + u_1v_0 + u_1v_1)$ . Equation (3) on p. 38 should read:

 $au_n + bu_m = 0$ 

(38)

$$au_{n+1}^{n} + bu_{m+1}^{n} = 0$$

On p. 42, 11 lines from the end, change the "F" to a script  $\Im$ .

On p. 49, in the equation preceding Eq. (10), change  $\alpha_i$  to  $\omega_i$ .