

$$S = (1/3 + 1/5) + (1/5 + 1/7) + \cdots + (1/32717 + 1/32719)$$

be the sum of the sum of the reciprocals of all twinprimes below 2^{15} . Indicate which of the following inequalities is true:

$$(a) \quad S < \pi^2/6 \qquad (b) \quad \pi^2/6 < S < \sqrt{e} \qquad (c) \quad \sqrt{e} < S.$$

Solutions by Paul Sands, Student, University of New Mexico, Albuquerque, New Mexico, and the proposer. (Both used electronic computers.)

	<u>Proposer</u>	<u>Paul Sands</u>
True inequality	(b)	(b)
Number of pairs of primes involved	55	55
S, to six decimal places	1.647986	1.648627

(Continued from p. 210.)

6.

$$T_n = -(-i)^n$$

7.

$$T_{n+1} = 5T_n - 6T_{n-1}$$

$$T_n = 2^n + 3^{n-1}$$

8.

$$r = \frac{5 + \sqrt{29}}{2}, \quad s = \frac{5 - \sqrt{29}}{2}$$

$$T_n = \frac{r^n - s^n}{\sqrt{29}} \quad \text{with terms } 1, 5, 26, 135, \dots$$

$$V_n = r^n + s^n \quad \text{with terms } 5, 27, 140, \dots$$

9.

$$r = \frac{3 + i\sqrt{11}}{2}, \quad s = \frac{3 - i\sqrt{11}}{2}$$

$$T_n = \left(\frac{33 - 16i\sqrt{11}}{55} \right) r^n + \left(\frac{33 + 16i\sqrt{11}}{55} \right) s^n$$

10.

$$T_{n+1} = 5T_n + 2T_{n-1}; \quad T_1 = 3, \quad T_2 = 7.$$
