and, for a = b, c = 0, to

$$(23) \quad \beta_{mn} = \frac{1}{p - q} \, (p\beta_n - q\beta_m) \qquad\qquad (m,n \geq 0; \; \beta_{mn} = \beta_{m+n} \in D).$$

A formula analogous to (23) is known in the operational calculus for functions of two continuous variables (see perhaps [7]; p,q difference operators) in the theory of two-dimensional Laplace transformation (see [8]).

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